

Abstract Submitted  
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**Isometric Families of Minimal Surfaces**<sup>1</sup> STEPHEN TAYLOR, BYU  
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TION — We consider a minimal surface  $M$  immersed in  $R^3$  with induced metric  
 $g = \psi\delta_2$  where  $\delta_2$  is the two dimensional Euclidean metric and  $2\psi$  is a scalar. We  
then construct a system of partial differential equations that constrain  $M$  to lift to a  
minimal surface via the Weierstrauss- Enneper representation demanding the metric  
is of the above form. It is concluded that associated surfaces connecting the pre-  
scribed minimal surface and its conjugate surface satisfy the system. Moreover, we  
find a non-trivial symmetry of the system that generates a one parameter family of  
surfaces isometric to a specified minimal surface. We demonstrate an instance of the  
analysis for the catenoid ( $\psi = \cosh^2(v)$ ), and comment on potential generalizations  
to a Lorentzian manifolds in a general relativistic setting.

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