Abstract Submitted for the APR06 Meeting of The American Physical Society

Analysis of the Lev Ginzburg Equation¹ MICHAEL BELLAMY, RONALD MICKENS, Clark Atlanta University — A second-order differential equation taking the form

 $(*) \qquad \qquad \ddot{x} = f(x, \dot{x}, p)$

was derived by Ginzburg¹. In this ODE, \dot{x} and \ddot{x} represent the first and second derivatives with respect to time; and p stands for four parameters, $p = (p_1, p_2, p_3, p_4)$, where (p_1, p_2, p_3) are non-negative and p_4 can be of either sign. The function f is linear in x, but quadratic in \dot{x} . Ginzburg's main purpose in constructing this equation was to take into consideration the "inertial behavior of biological populations." However, this ODE can also be used to model a variety of physical dynamical systems.² With four parameters, there is a broad range of possible solution behaviors. Our present purpose is to prove that limit-cycle behavior can occur for Eq. (*) under the appropriate conditions on the parameters. We demonstrate this result by means of the Hopf bifurcation theory.³ References ¹L. Ginzburg and M. Colyvan, Ecological Orbits (Oxford, New York, 2004). ²S. H. Strogatz, Nonlinear Dynamics and Chaos (Addison-Wesley; Reading, MA; 1994). ³E. Beltrami, Mathematics for Dynamic Modeling (Academic Press, Boston, 1987).

¹Research supported in part by grant from DOE and Title III Funds at Clark Atlanta University.

Ronald Mickens Clark Atlanta University

Date submitted: 09 Jan 2006

Electronic form version 1.4