

Abstract Submitted  
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**The complete set of Casimirs in Hall-MHD**<sup>1</sup> YOHEI KAWAZURA,  
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A procedure to determine all Casimir constants of motion in MHD<sup>2</sup> is extended  
to Hall-MHD. We obtain differential equations for the variational derivatives of all  
Casimirs which must be satisfied for any dynamically accessible motion of Hall-  
MHD. In an extension of the more commonly considered model, we also include  
the electron fluid entropy. The most interesting case, usually true for axisymmetric  
configurations, is when both the electron and ion entropy functions form families  
of nested toroidal surfaces. The Casimirs are then three functions of each of the  
entropies, involving fluxes of certain vector fields and the number of particles con-  
tained in each torus. If any of the species loses its nested tori, the number of the  
associated Casimirs is much larger (but physically less relevant).

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<sup>2</sup>E. Hameiri, *Phy. Plasmas*, **11**, 3423 (2004).

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