

Abstract Submitted  
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**Stokes' Parameters Compared to Astrophysical Magnetic Turbulence Parameters** MIRIAM FORMAN, Stony Brook University, ROBERT WICKS, NASA/Goddard Space Flight Center, SEAN OUGHTON, Waikato University, NZ, TIMOTHY HORBURY, Imperial College, UK — Since the divergence of a magnetic field is zero, the Fourier transform of fluctuations  $\delta\mathbf{B}(\mathbf{k})$  must be perpendicular to  $\mathbf{k}$ , so  $\delta\mathbf{B}(\mathbf{k})$  has components only in the plane perpendicular to  $\mathbf{k}$ . When there is also a mean field  $\mathbf{B}$ , the obvious choice of coordinates to describe  $\delta\mathbf{B}(\mathbf{k})$  are the unit vectors  $\mathbf{t}$  in the direction  $\mathbf{B} \times \mathbf{k}$  and  $\mathbf{p}$  in the direction  $(\mathbf{B} \times \mathbf{k}) \times \mathbf{k}$ , called the “toroidal” and “poloidal” directions, respectively. Oughton, et al. (1997) as elucidated by Wicks et al. (2012) showed that the power spectral tensor  $P_{ij}(\mathbf{k})$  of magnetic fluctuations is described by four scalar functions of  $\mathbf{k}$ , multiplying the tensors  $\mathbf{t}:\mathbf{t}$ ,  $\mathbf{p}:\mathbf{p}$ ,  $\mathbf{t}:\mathbf{p}+\mathbf{p}:\mathbf{t}$ , and  $\mathbf{t}:\mathbf{p}-\mathbf{p}:\mathbf{t}$  so that the Hermitian  $P_{ij}(\mathbf{k}) = \text{Tor}(\mathbf{k}) \mathbf{t}:\mathbf{t} + \text{Pol}(\mathbf{k}) \mathbf{p}:\mathbf{p} + C(\mathbf{k}) [\mathbf{t}:\mathbf{p}+\mathbf{p}:\mathbf{t}] + i\mathbf{k}H(\mathbf{k}) [\mathbf{t}:\mathbf{p}-\mathbf{p}:\mathbf{t}]$ . Since the electromagnetic fluctuations  $\delta\mathbf{B}(\mathbf{k})$  and  $\delta\mathbf{E}(\mathbf{k})$  in a beam of light are also perpendicular to their  $\mathbf{k}$ , the four scalar functions of magnetic turbulence in astrophysics which scatters cosmic rays and allows their acceleration, are analogs of the Stokes' parameters. Using Chandrasekhar's (1960) notation  $[I, Q, U, V]$ :  $I = \text{Tor} + \text{Pol} = \text{Tr}(P_{ij}(\mathbf{k}))$ ;  $Q = \text{Tor} - \text{Pol}$ ;  $U = C$ ; we speculate that  $V$  corresponds to magnetic helicity  $\mathbf{k}H$  in turbulence. We are studying projections of  $P_{ij}(\mathbf{k})$  observed by spacecraft in the solar wind.

Miriam Forman  
Stony Brook University

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