Spontaneous mass generation and the small dimensions of the
Standard Model gauge groups $U(1)$, $SU(2)$ and $SU(3)$

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