

Abstract Submitted
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Monodromy? What's Monodromy?¹ J.B. DELOS, William and Mary,
D. SADOVSKII, B. ZHILINSKII, Universite Littoral — We say that a system exhibits *monodromy* if we take the system around a closed loop in its parameter space, and we find that the system does not come back to its original state. Many systems have this property: atoms in a trap, a hydrogen atom in crossed fields, electronic states of H_2^+ , and vibrational states of CO_2 . Imagine noninteracting classical particles moving in a two-dimensional circular box with a hard reflecting wall, and with a cylindrically-symmetric potential energy barrier: $\rho = (x^2+y^2)^{1/2}$, $[V(\rho) = -a \rho^2/2, \rho < R], [V(\rho)=\text{infinity}, \rho \geq R]$. Start all the particles moving on one line with angular momentum $L=0$, and with energy $E < 0$. Then impose additional smooth forces and torques on the particles so that $[L(t), E(t)]$ moves in a circle around the origin in the $[L,E]$ plane. In other words, apply a torque to increase the angular momentum, then drive the particles to a higher energy (above the barrier), then reduce the angular momentum to a negative value, reduce the energy, and finally come back to the initial energy and angular momentum. Where in space do the particles end up? The answer is surprising.

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