Theoretical and numerical calculation of the Eddy viscosity in smooth and rough turbulent boundary layers

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