Non-robustness of the two-dimensional turbulent inverse cascade

RICHARD SCOTT, Northwest Research Associates — The inverse energy cascade in two-dimensional Navier-Stokes turbulence is examined in the quasi-steady regime, with small-scale, band-limited forcing at scale \( k_f^{-1} \). It is found that the forcing Reynolds number, \( Re \sim k_{max}^2/k_f^2 \), where \( k_{max} \) is the maximum resolved wavenumber, plays a crucial role in determining the energy distribution at larger scales. The strength of the inverse energy cascade, or fraction of energy input that is transferred to larger scales, increases monotonically towards unity with increasing \( Re \). Moreover, as \( Re \) increases beyond a critical value, for which a direct enstrophy cascade to small scales is first realized, the energy spectrum in the energy-cascading range steepens abruptly from a \( k^{-5/3} \) to \( k^{-2} \) dependence. The steepening is interpreted as the result of a greater tendency for coherent vortex formation in cases when forcing scales are adequately resolved, and is consistent with a small but nonzero net upscale enstrophy flux associated with near inviscid vortex merger. The results suggest the need for a review of the traditional interpretation and analysis of the inverse cascade.

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