Transport of densities in position-orientation space for the study of orientable particles in microchannels

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