Optimal Prandtl number for heat transfer in rotating Rayleigh-Bénard convection

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1Stichting Fundamenteel Onderzoek der Materie (FOM)
2Ahlers et al. Rev. Mod. Phys. 81, 503 (2009)