Supercritical Quasi-conduction States and Multiple Stable Flows in Stochastic Rayleigh-Bénard Convection

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