Effects of the mean velocity field on the renormalized turbulent viscosity and correlation function

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