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Critical Steady Surface Waves of Idea Fluid over a Bump with Surface Tension JEONGWHAN CHOI, SANGWON LEE, JOONKYOUNG KIM, Korea University, SUNGIM WHANG, Ajou University — The paper deals with steady forced surface waves propagating on a two-dimensional incompressible and inviscid fluid with a small bump placed on a rigid flat bottom. If the surface tension coefficient T on the free surface is not zero and the wave is moving with a constant speed C , the wave motion is determined by two non-dimensional constants, $F = gh$ and $\tau = T/(gh^2)$, where g is the gravity constant and h is the height of the fluid at infinity. It has been known that $F = 1$ and $\tau = 1/3$ are the critical values of F and τ , respectively. In the critical case $F = 1 + \epsilon^2$ and $\tau = 1/3 + \epsilon$ with $\epsilon \ll 1$ a small parameter, a time-dependent forced Kawahara (F-Kawahara) equation is derived to model the wave propagation on the free surface and the steady F-Kawahara equation is studied both theoretically and numerically. It is shown that the steady F-Kawahara equation has many different kinds of one and multi-hump solutions when ϵ and F vary. In particular, for a fixed ϵ , there is a $\tau_c > 0$ such that if $\tau > \tau_c$, two one-hump steady solutions can be obtained, one with small amplitude and the other with large amplitude. By using the unsteady F-Kawahara equation, it appears that the small one-hump solution is stable while the large one is unstable. In addition, two-hump solutions are unstable.

Jeongwhan Choi
Korea University

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