

Abstract Submitted  
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**Approximate Solutions to the Linearized Navier-Stokes Equations** ANTHONY LEONARD, California Institute of Technology — The linearized Navier-Stokes equations for incompressible channel flow are considered in which the flow is homogeneous in two directions. We study the initial-value problem for  $v$  and  $\omega_y$ , where  $y$  is the coordinate normal to the wall. After a Laplace transform in time and a double Fourier transform in space we use the WKB approximation on the resulting system of ODEs in  $y$ . For example, for the inviscid equations we can construct analytically the Greens function for such solutions in terms of the Bessel functions  $J_{+1/3}$ ,  $J_{-1/3}$ ,  $J_1$ , and  $Y_1$  and their modified counterparts. In this approach the critical layer or the  $y$  location where  $U(y) = \omega/k_x$  requires special attention, as might be expected, as well as the location of the turning point where  $d^2U/dy^2 = (k_x^2 + k_z^2)(\omega/k_x - U(y))$ , if it exists.

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