Automatic-differentiated shadowing methods for optimization and data assimilation of chaotic acoustics

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