

Abstract Submitted  
for the DPP06 Meeting of  
The American Physical Society

**Numerical algorithms for cold-relativistic plasma models in the presence of discontinuities**<sup>1</sup> AMMAR HAKIM, JOHN CARY, DAVID BRUH-WILER, Tech-X Corporation, Boulder CO, 80303, CAMERON GEDDES, WIM LEEMANS, ERIC ESAREY, Lawrence Berkley National Lab. — A numerical algorithm is presented to solve cold-relativistic electron fluid equations in the presence of sharp gradients and discontinuities. The intended application is to laser wake-field accelerator simulations in which the laser induces accelerating fields thousands of times those achievable in conventional RF accelerators. The relativistic cold-fluid equations are formulated as non-classical system of hyperbolic balance laws. It is shown that the flux Jacobian for this system can not be diagonalized which causes numerical difficulties when developing shock-capturing algorithms. Further, the system is shown to admit generalized delta-shock solutions, first discovered in the context of sticky-particle dynamics (Bouchut, *Ser. Adv. Math App. Sci.*, **22** (1994) pp. 171–190). A new approach, based on relaxation schemes proposed by Jin and Xin (*Comm. Pure Appl. Math.* **48** (1995) pp. 235–276) and LeVeque and Pelanti (*J. Comput. Phys.* **172** (2001) pp. 572–591) is developed to solve this system of equations. The method consists of finding an exact solution to a Riemann problem at each cell interface and coupling these to advance the solution in time. Applications to an intense laser propagating in an under-dense plasma are presented.

<sup>1</sup>Work supported by the Office of High Energy Physics

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Date submitted: 21 Jul 2006

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