

Abstract Submitted  
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**The Redmond Formula with Seniority** LARRY ZAMICK, ALBERTO ESCUDEROS, Rutgers U. — As we get to heavier nuclei, we find more states with different seniorities and several states of a given seniority. There is a recursion formula by Redmond that relates an  $n \rightarrow (n + 1)$  coefficient of fractional parentage (cfp) to that of  $(n - 1) \rightarrow n$ . However, this involves an *overcomplete* set of principal parent (pp) cfp's. For example, for a 3-particle system, we can form basis states  $[[12]^{J_0}3]^J$ , where  $J_0$  is the pp; we then antisymmetrize and normalize  $\Psi[J_0] = N[J_0](1 - P_{12} - P_{13}) [[12]^{J_0}3]^J$ , and form a ppcfp expansion  $\Psi[J_0] = \sum_{J_1} [j^2(J_1)j] \{j^3[J_0]J\} [[12]^{J_1}3]^J$ . But for, say,  $J = j = 9/2$ , there are five  $\Psi[J_0]$ 's, but only two independent wave functions, one with seniority 1 and one with seniority 3. We note that  $[j^2(J_0)j] \{j^3[J_0]J\} = 1/(3N[J_0])$ . We are able then to obtain the following relation between overcomplete ppcfp's and complete orthonormal cfp's:  $A = B = C$ , where

$$\begin{aligned}
 A &= (n + 1) [j^n(J_0 v_0)j] \{j^{n+1}[J_0 v_0]J\} [j^n(J_1 v_1)j] \{j^{n+1}[J_0 v_0]J\}, \\
 B &= (n + 1) \sum_v [j^n(J_0 v_0)j] \{j^{n+1}Jv\} [j^n(J_1 v_1)j] \{j^{n+1}Jv\}, \\
 C &= \delta_{J_0 J_1} \delta_{v_0 v_1} + n(-1)^{J_0 + J_1} \sqrt{(2J_0 + 1)(2J_1 + 1)} \sum_{v_2 J_2} J_2 j J_1 J j J_0 \times \\
 &\quad \times [j^{n-1}(J_2 v_2)j] \{j^n J_0 v_0\} [j^{n-1}(J_2 v_2)j] \{j^n J_1 v_1\}.
 \end{aligned}$$

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