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Flow Equation Approach to the Statistics of Nonlinear Dynamical Systems J.B. MARSTON, SEUNGWOOK MA¹, Brown University, M.B. HASTINGS², Los Alamos National Laboratory — The probability distribution function of non-linear dynamical systems is governed by a linear framework that resembles quantum many-body theory, in which stochastic forcing and/or averaging over initial conditions play the role of non-zero \hbar . Besides the well-known Fokker-Planck approach, there is a related Hopf functional method³; in both formalisms, zero modes of linear operators describe the stationary non-equilibrium statistics. To access the statistics, we investigate the method of continuous unitary transformations⁴ (also known as the flow equation approach⁵), suitably generalized to the diagonalization of non-Hermitian matrices. Comparison to the more traditional cumulant expansion method is illustrated with low-dimensional attractors. The treatment of high-dimensional dynamical systems is also discussed.

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³Uriel Frisch, *Turbulence: The Legacy of A. N. Kolmogorov* (Cambridge University Press, 1995) chapter 9.5.
⁴S. D. Glazek and K. G. Wilson, Phys. Rev. D 48, 5863 (1993); Phys. Rev. D 49, 4214 (1994).
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