Thermally activated escape rate for a Brownian particle in a tilted periodic potential for all values of the dissipation: classical and quantum regimes

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