The search for minimum-energy atomic configurations on a lattice: Lamarckian twist on Darwinian Evolution

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