Experimental Realization of Adaptive Qubit Tomography

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\cite{1} Phys. Rev. A 78, 052122 (2008)
\cite{2} Phys. Rev. Lett. 97, 130501 (2006)