

Abstract Submitted
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Supersymmetric Structure of two Families of Solitons¹ ANDREW KOLLER, MAXIM OLSHANII, University of Massachusetts Boston — Solitons have generated considerable interest in the cold atoms and condensed matter communities. We demonstrate that two families of n -soliton solutions (with n an integer) – one for the attractive nonlinear Schrödinger (NLS) equation, and one for the sine-Gordon (sG) equation – originate from a quantum-mechanical supersymmetric (QM-SUSY) chain connecting a set of reflectionless operators \hat{H}_n . The families consist of breather-type solitons for NLS² and multi-(anti)kink solitons with specific velocities for sG. The operators \hat{H}_n , which we refer to as Akulin’s Hamiltonians³, form reflectionless direct-scattering initial conditions for the inverse scattering method. Such a QM-SUSY chain is analogous to the known connection between QM-SUSY chains of Pöschl-Teller potentials and solitons of the Korteweg-de Vries (KdV) equation⁴. The existence of QM-SUSY chains connecting soliton solutions, now for three different integrable nonlinear equations, sheds light on the underlying mechanisms responsible for soliton generation.

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