

Abstract Submitted  
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**Scaling of Minimum Dominating Sets in Various Scale-Free Network Ensembles**<sup>1</sup> F. MOLNAR, S. SREENIVASAN, B.K. SZYMANSKI, G. KORNISS, Rensselaer Polytechnic Institute — We study the scaling behavior of the size of minimum dominating sets (MDS) in scale-free networks, with respect to network size  $N$  and power-law exponent  $\gamma$  [Nacher et al., NJP 073005 (2012)]. Network samples are constructed by either the configuration model (CM) via multigraphs, or exact degree sequence sampling methods. The MDS is found by a sequential greedy algorithm. We control the average degree by setting an appropriate lower degree cutoff  $k_{\min}$ . Two subtypes of networks are studied according to the maximum degree cutoff  $k_{\max}$ . Our results show that when  $k_{\max} = \sqrt{N}$  all networks have similar scaling. The size of MDS is linear with respect to  $N$ , and for a given  $N$ , it increases for low  $\gamma$  values. When  $k_{\max} = N - 1$ , we find a structural difference between CM networks, and networks constructed by exact sampling methods. For the latter, we find a scaling transition of the MDS size from  $O(N)$  to  $O(1)$  at approximately  $\gamma \approx 1.9$ , due to the appearance of star subgraphs with  $O(N)$  central degree. For a given  $N$ , the size of MDS increases for higher  $\gamma$  values. However, in CM networks the MDS scales linearly with  $N$ , and for a given  $N$ , it is non-monotonic with respect to  $\gamma$ . Finally, we find that a partial MDS, which dominates only a certain fraction of the network, has the same scaling as full domination, even for as low as 30% dominated fraction.

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