Renormalization Group for Quantum Walks

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2http://www.physics.emory.edu/faculty/boettcher/
3http://www.lncc.br/~portugal/