Numerical study of the butterfly effect on the solutions of the logistic difference equation using arbitrary significant digits

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