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**Full analytical Expressions of the Quantum Mechanical Energy Eigenstates of charged Particles confined in a Penning Trap at non-relativistic Energies.** ERIC STEINFELDS, KEITH ANDREW, Western Kentucky University — The storage of a few charged particles at low kinetic energy and at higher energies can be estimated by finding and characterizing the trajectories of charged particles which are classically bound within a Penning trap. However, there is benefit to using quantum mechanics to predict the energy levels and to map out the probability distributions of a few charged particles such as e's and protons which are 'trapped' in a given Penning Trap with particular settings for  $B_0$  (magnetic field) and quadrupole 'E'strength ( $V_{zz[qua]}$ ). We are able to analytically solve the Schrödinger equation which represents the Hamiltonian of a single charged particle confined in a Penning 'device'. Presuming that the  $L_{[orbit]}$  and 'longitudinal' kinetic energies are non-relativistic, then the eigenvalues of the possible energies of the single charged particle follows a formula for "QM" integers  $N$  and  $m$ :  $E_{(N,m)} = 2*\hbar/M*G*(N+1) -m*\hbar*q*Bo/M$ , where  $G = \sqrt{q^2*Bo^2/4 -M/2*q*V_{zz[qua]}}$ . This work matches the formulation the famous QM text [1]. On the other hand, ref[1] allows  $B_0$  but not  $V_{zz[qua]}$ .

Bibliography:

[1] L. Landau and E. Lifshitz, "Quantum Mechanics Course of Theoretical Physics", Volume 3-Third Edition, Pergamon Press, 1977.

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