

Abstract Submitted  
for the SHOCK05 Meeting of  
The American Physical Society

**A Rate-Dependent Damage Model and its Application to Uniaxial Strain** MARTIN N. RAFTENBERG, MICHAEL A. GRINFELD, U.S. Army Research Laboratory — Our analysis is based on a damage model discussed in [1] in which the internal energy density  $W$  depends on strain  $\mathbf{E}$  and damage  $\kappa$  :  $W(\mathbf{E}, \kappa) = \phi(\kappa) \mu \left( \frac{\nu}{1-2\nu} E_{kk} E_{ll} + E_{ij} E_{ij} \right)$ ;  $\mu$  is elastic shear modulus,  $\nu$  is Poisson's ratio. The factor  $\phi(\kappa) = 1 - (1 - \phi_{\min}) \frac{\kappa}{\kappa_{\max}}$  describes degradation of elastic modulus due to damage;  $\phi_{\min}$  and  $\kappa_{\max}$  are material constants. The system of evolution includes

$$\rho \frac{\partial^2 u}{\partial t^2} = \nabla \frac{\partial W}{\partial \mathbf{E}}, \quad \frac{\partial \kappa}{\partial t} = -K \frac{\partial W}{\partial \kappa}$$

where  $K$  is (for now) a material constant. The above model was installed into LS-DYNA using the User Material Interface. The model was applied to a finite-element simulation of a rod under uniaxial strain, with a prescribed-velocity boundary condition at one end and a stress-free condition at the other. The resulting initial-value boundary-value problem was scaled to reveal the presence of the dimensionless group  $\Pi = \frac{\rho_0}{2} \sqrt{\frac{(1-2\nu)\rho_0}{2(1-\nu)\mu} \cdot \frac{(1-\phi_{\min})K}{\kappa_{\max}^2}} \cdot L \cdot \dot{u}_0^2$ , where  $\rho_0$  is the material density,  $L$  is the length of the rod, and  $\dot{u}_0$  is the prescribed velocity. Solutions were obtained for a range of  $\Pi$  values. The progression of contours of  $\kappa(x,t)$  was observed. [1] Grinfeld, M.A., and Wright, T.W., *Metallurgical and Materials Transactions A*, Vol. 35A, 2651-2661, 2004.

Martin N. Raftenberg  
U.S. Army Research Laboratory

Date submitted: 07 Apr 2005

Electronic form version 1.4