Abstract Submitted for the TSS15 Meeting of The American Physical Society

Solar peak color in human eye¹ LIANXI MA, Blinn College — There are two forms of Wien's displacement law that can be derived from Planck's equation. They are: $\lambda_m T = \text{constant}(1)$ and $\frac{f_m}{T} = \text{constant}(2)$ Suppose that we have known a black body's temperature, then $\lambda_{\rm m}$ and $f_{\rm m}$ can be obtained from Eqs. (1) and (2). For example, the Sun's surface temperature, T = 5778 K, then according to Eq. (1) $\lambda_{\rm m}$ = 500 nm which is green; but according to Eq. (2) $f_{\rm m}$ = 3.40 × 10^{14} Hz which is near-infrared. While the inequality $\lambda_m f_m \neq c$ can be explained mathematically by substituting $\lambda f = c$ into Planck's radiation function, the question lingers: what color of sun light "really" peaks in human eye? The answer is that Planck's function, or Wien's law, can't answer this question. Planck's function, $I(\lambda)$, or I(f), is the radiation intensity per $d\lambda$ (meter) or df (Hz) and, $d\lambda$ and df don't have same interval. For a spectrometer, it peaks at green if λ changes evenly; peaks at near-infrared if f changes evenly. For human eye, its peak's location depends on $I(\lambda)$, or I(f), and, how much each type of cone is excited. We can naively represent any color as a triplet of numbers: (red, green, blue), where each is the degree to which the associated type of cone is excited. Then red = $\int d\lambda I(\lambda) S_r(\lambda) = \int df I(f) S_r(f)$ -(3) where $S_r(\lambda)/S_r(\lambda)$ is the sensibility of red cone. For green and blue we have same equations. Then the peak is determined by the value of integral.

¹Thanks to D. Goldhaber-Gordon, and D. Zimmerman

Lianxi Ma Blinn College

Date submitted: 06 Feb 2015

Electronic form version 1.4