

Abstract Submitted  
for the DAMOP13 Meeting of  
The American Physical Society

**Lee-Yang cluster expansion approach to BCS-BEC crossover**

NAOYUKI SAKUMICHI, Department of Physics, The University of Tokyo,  
YUSUKE NISHIDA, Theoretical Division, Los Alamos National Laboratory,  
MASAHITO UEDA, Department of Physics, The University of Tokyo — A dilute gas of spin-1/2 Fermi atoms can continuously evolve from Cooper pairing to Bose-Einstein condensation (BEC) of tightly-bound dimers by changing the strength of interaction between them. This is called BCS-BEC crossover and has realized by using a ultracold atomic gases. In this work, we propose a new systematic approach to describe the BCS-BEC crossover based on a cluster expansion method of Lee and Yang. Here, the cluster expansion is a systematic expansion of the equation of state in terms of the fugacity  $z := e^{\beta\mu}$  as  $\beta\lambda^3 p = 2z + b_2 z^2 + b_3 z^3 + \dots$ , with inverse temperature  $\beta = (k_B T)^{-1}$ , chemical potential  $\mu$ , pressure  $p$ , and thermal de Broglie length  $\lambda := (2\pi\hbar\beta/m)^{1/2}$ . We show the following results: (i) in the weak-coupling limit, the Thouless criterion and the number equation of Nozieres and Schmitt-Rink are derived, and thereby the critical temperature is identical with that of the BCS theory; (ii) in the strong-coupling limit, the critical temperature is identical with that of the BEC of non-interacting dimers; (iii) The exact second cluster integral  $b_2$ , which is dominant in the high-temperature region, is also included in the expansion for any value of an s-wave scattering length  $a$ .

Naoyuki Sakumichi  
Department of Physics, The University of Tokyo

Date submitted: 30 Jan 2013

Electronic form version 1.4