

Abstract Submitted  
for the DAMOP15 Meeting of  
The American Physical Society

**Sum rules for spin-1/2 quantum gases in well-defined-spin states**

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[1] V.A. Yurovsky, Phys. Rev. Lett. **113**, 200406 (2014).

[2] V.A. Yurovsky, arXiv:1501.06182.

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Date submitted: 28 Jan 2015

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