

Abstract Submitted  
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**Particle Number and Probability Density Functional Theory, and A-representability**<sup>1</sup> VIRAHT SAHNI, Brooklyn College, CUNY, XIAOYIN PAN, Ningbo University, China — In Hohenberg-Kohn (HK) density functional theory (DFT), the functional  $F_{HK}[\rho]$  of the density  $\rho(\mathbf{r})$  representing the expectation of the electron-interaction and kinetic energy operators is universal. Knowledge of  $F_{HK}[\rho]$  by itself is insufficient to obtain the energy: the electron number  $N$  is primary. By emphasizing this primacy of  $N$ , we rewrite the energy  $E$  as a nonuniversal functional of  $N$  and probability density  $p(\mathbf{r}) : E = E[N, p]$ , with  $p(\mathbf{r})$  satisfying the constraints of normalization to unity and positivity. A particle number  $N$  and probability density  $p(\mathbf{r})$  functional theory is constructed, and examples of exact functionals provided. The concept of  $A$ -representability is introduced as the set of functions  $\psi_p$  that lead to quantum mechanical  $p(\mathbf{r})$  as the expectation of the probability density operator. We show via the Harriman and Gilbert constructions that the  $A$ - and  $N$ -representable probability density  $p(\mathbf{r})$  sets are equivalent, with the latter defined as  $p(\mathbf{r}) = \rho(\mathbf{r})/N$ .

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Virahht Sahni  
Brooklyn College, CUNY

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