

Abstract Submitted  
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**Probing Collins conjecture with correlation energies and entanglement entropies for the ground state of the helium isoelectronic sequence**<sup>1</sup> YEW KAM HO, YEN-CHANG LIN, Institute of Atomic and Molecular Sciences, Academia Sinica — Correlation energy of a quantum system is defined as the difference between its exact energy  $E_{\text{ex}}$ , and its Hartree-Fock energy  $E_{\text{HF}}$ . In a recent related development, entanglement measures can be quantified with von Neumann entropy  $S_{vN}(\rho) = -\text{Tr}(\rho \log_2 \rho)$  or linear entropy  $S_L(\rho) = 1 - \text{Tr}(\rho^2)$ , where  $\rho$  is the one-particle reduced density matrix, and  $\text{Tr}(\rho^2)$  is defined as the purity of state. In the present work we calculate  $S_L$  and  $S_{vN}$  for the ground  $1s^2 1S$  states in helium-like ions for  $Z = 2$  to 15, using configuration interaction (CI) with  $B$ -Spline basis up to about 6000 terms to construct the wave functions, and with which density matrix, linear and von Neumann entropies are calculated [1]. We have found close relationship between the reduced correlation energy, defined as  $E_{\text{corr}} = (E_{\text{CI}} - E_{\text{HF}})/E_{\text{CI}}$  (with  $E_{\text{CI}}$  being our calculated energy), and  $S_L$  or  $S_{vN}$ . Our results support Collins conjecture [2] that there is a linear relationship between correlation energy and entanglement entropy, i.e.,  $E_{\text{corr}} = CS$ , where  $C$  is called Collins constant. Using the calculated ground state energies for  $Z = 2$  to  $Z = 15$ , and the entanglement measured with linear entropy  $S_L$  for such states,  $C$  is determined as 0.90716. At the meeting, we will present result for Collins constant determined from von Neumann entropy, and details of our calculations. [1] Y.-C. Lin, C.-Y. Lin, and Y. K. Ho, *Phys. Rev. A* **87**, 022316 (2013); *Can. J. Phys.* **93**, 646 (2015). [2] D. M. Collins, *Z. Naturforsch.*, **48**, 68 (1993).

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