Observation of out-of-plane vibrations in few-layer graphene using combination and overtone Raman modes  
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